

Quantifying the inactivation rate constants for the molecular species comprising the catalytic cycle of *Leuconostoc mesenteroides* glucose 6-phosphate dehydrogenase

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Abstract

When an unstable enzyme is incubated with its substrate(s), catalysis may cease before chemical equilibrium is attained. The residual substrate concentrations depend on their initial concentrations, the initial enzymic activity, and the inactivation rate constants for each molecular species that comprise the catalytic cycle. The underlying theory has been elaborated previously for single-substrate reactions and here it is extended to bi-substrate reactions. The theory is illustrated by application to glucose 6-phosphate dehydrogenase, which is unstable when exposed to a low concentration of sodium dodecyl sulphate. It is shown that the ternary complex containing both substrates is resistant to inactivation while each of the remaining complexes undergoes first-order decay. Rate constants for the inactivation of each complex are calculated.

Keywords: *Bi-substrate reaction, enzyme inactivation, glucose 6-phosphate dehydrogenase, rate constant, residual substrate, unstable enzyme*

Abbreviations: *G6P, glucose 6-phosphate; SDS, sodium dodecyl sulphate*

Introduction

When an enzyme is incubated with its substrate(s), catalysis normally proceeds until the substrates and products are in chemical equilibrium. If the reaction is nearly irreversible, this equilibrium will approximate exhaustion of the limiting substrate. This simple property is used widely for the estimation of biochemical compounds.

If the enzyme is unstable, its activity will decline over time leading to the possibility that all activity is lost before chemical equilibrium is attained. In these circumstances there will be some residual substrate even when the catalyzed reaction itself is irreversible. Previous work by this author [1] and others [2] has developed the basic theory and equations for this situation for enzymes catalyzing single-substrate reactions.

One of the outcomes of this theory is specific predictions about the effects of variations in the initial

substrate concentration and the initial enzymic activity on the residual concentration of substrate. From these measurements it is possible to quantify the inactivation rates of various complexes along the catalytic pathway. This theory has been applied to, and extended for, several enzymes [3–12]. For example, alkaline phosphatase is inactivated by metal-chelating agents [3]. It was shown that the essential zinc ion is only accessible in the free enzyme; it is locked into the enzyme-substrate and enzyme-phosphate complexes of the catalytic cycle, making these resistant to inactivation by chelators. Of particular interest are mechanism-based inhibitors (“suicide substrates”), which inactivate a catalytic intermediate without affecting the free enzyme. A recent example of this is illustrated by the effect of hydroxypyruvate on acetohydroxacid synthase [10].

To date, the theory has been applied mainly to enzymes catalyzing single-substrate reactions, or to

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ones where the effect of any second substrate can be ignored. Here I develop a general extension to bi-substrate reactions and illustrate the theory with some results on the inactivation of *Leuconostoc mesenteroides* glucose 6-phosphate (G6P) dehydrogenase.

Theory

The basic mechanism that is considered here is shown in Scheme 1. It is assumed explicitly that the conversion of EAB to EQ is irreversible, which may result from the irreversible release of product P, or its removal by a coupling reaction. In the specific case of G6P dehydrogenase, the overall reaction is irreversible due to the rapid and spontaneous hydrolysis of the 6-phosphoglucono- δ -lactone product.

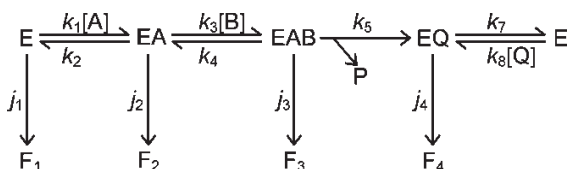
Each of the complexes on the catalytic pathway is subject to inactivation in a first-order manner, being converted to the inactive forms F_1 to F_4 with rate constants j_1 to j_4 , respectively. It does not matter whether F_1 to F_4 are identical, or if they differ from one another either in conformation or molecular composition. The rate of catalysis (v) for the ordered Bi Bi mechanism [13] can be simplified by setting $[P] = 0$, giving Equations (1–3) in which $[E]'_o$ is the total concentration of active enzyme (i.e. that which has not decayed to $F_1 - F_4$). The kinetic constants K_a , K_b , K_{ia} and K_{iq} have their conventional definitions [13].

$$v = k_c[E]'_o/\Delta \quad (1)$$

$$k_c = k_5k_7/(k_5 + k_7) \quad (2)$$

$$\Delta = 1 + K_b/[B] + (K_a/[A] + K_{ia}K_b/[A][B]) (1 + [Q]/K_{iq}) \quad (3)$$

In order to derive an expression for the total rate of enzyme inactivation, it is necessary to know the fraction of the enzyme that is present as each of the four species on the catalytic pathway. These fractions



Scheme 1. Inactivation mechanism of a bi-substrate enzyme-catalyzed reaction. The conventional catalytic pathway for an ordered sequential mechanism is shown at the top, with the conversion of EAB to EQ taken to be irreversible. This could occur by release of a product that is then removed by further reaction. Each discrete enzyme species is capable of undergoing conversion to the inactive species F_1 to F_4 , at rates governed by the rate constants j_1 to j_4 , respectively.

are given as Equations (4–7) where λ is the dimensionless quantity $k_5/(k_5 + k_7)$.

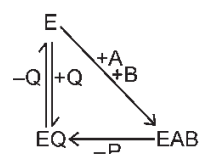
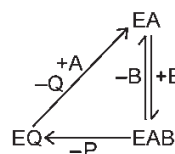
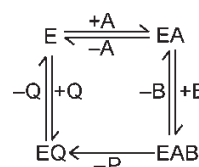
$$[E]/[E]'_o = (K_a/[A] + K_{ia}K_b/[A][B])/\Delta \quad (4)$$

$$[EA]/[E]'_o = (K_b/[B])/\Delta \quad (5)$$

$$[EAB]/[E]'_o = (1 - \lambda)/\Delta \quad (6)$$

$$[EQ]/[E]'_o = (K_a[Q]/K_{iq}[A] + K_{ia}K_b[Q]/K_{iq}[A][B] + \lambda)/\Delta \quad (7)$$

Using Equations (1–7) it is possible to write differential equations for the time dependence of substrate concentrations (e.g. $d[A]/dt$) and active enzyme ($d[E]'_o/dt$). However, these equation cannot be solved algebraically because $d[A]/dt$ depends upon $[E]_o$ and $d[E]'_o/dt$ depends upon $[A]$. As outlined by Duggleby [1], the two differential equations can be combined to obtain an expression for the change in enzyme activity relative to the change in the substrate concentration (i.e. $d[E]'_o/d[A]$). Integrating and setting $[E]'_o = 0$ defines residual substrate concentration when all enzymic activity has been lost and catalysis ceases. This can be done for any initial concentration of substrates and enzyme but it is more useful to consider some limiting cases that can be set up in practice. These are a saturating concentration of substrate A, and a saturating concentration of substrate B. The effects of these simplifying conditions are illustrated in Scheme 2. When neither



Scheme 2. Simplifications of the mechanism of a bi-substrate enzyme-catalyzed reaction. The conventional catalytic cycle for Scheme 1 is shown in the top panel. Saturation with substrate A effectively removes free enzyme (E) from the cycle (middle panel), while saturation with substrate B results in direct conversion of E to EAB (bottom panel).

substrate is saturating, the catalytic cycle is as represented in the upper panel of Scheme 2. However, saturating with A (middle panel, Scheme 2) means that when EQ releases Q to form E, this will be converted immediately and irreversibly to EA. Effectively, there is a single irreversible step where EQ is converted directly to EA. Similarly, saturating with B (bottom panel, Scheme 2) results in the conversion of E to EAB in a single irreversible step. The relevant equations for these two situations will now be developed.

Saturating [A]. When the concentration of substrate A is much greater than both K_a and K_{ia} , Equations (1–7) are greatly simplified as shown by Equations (8) and (9). Expressions for v , $[EA]/[E]'_o$ and $[EAB]/[E]'_o$ are not shown as they are identical Equations (1), (5) and (6) except for the replacement of Δ by Δ_a , while $[E]/[E]'_o = 0$.

$$\Delta_a = 1 + K_b/[B] \quad (8)$$

$$[EQ]/[E]'_o = \lambda/\Delta_a \quad (9)$$

Using these relationships, we may write an expression for the change in enzyme activity relative to the change in the concentration of the non-saturating substrate, B. This is given as Equation (10).

$$d[E]'_o/d[B] = (j_2K_b/[B] + j_3(1 - \lambda) + j_4\lambda)/k_c \quad (10)$$

Integrating Equation (10) and setting $[E]'_o = 0$ yields an expression (Equation 11) that relates $[B]_f$, the residual concentration of substrate B, to its initial concentration ($[B]_o$), and the original amount of enzyme before inactivation ($[E]_o$).

$$\frac{V_m}{[B]_o - [B]_f} = j_2K_b \frac{\ln([B]_o/[B]_f)}{[B]_o - [B]_f} + j_b \quad (11)$$

In Equation (11), V_m equals $k_c[E]_o$ while j_b is a composite inactivation rate constant that is defined by Equation (12).

$$j_b = j_3(1 - \lambda) + j_4\lambda \quad (12)$$

It is evident from Equation (11) that a plot of $V_m/([B]_o - [B]_f)$ against $\ln([B]_o/[B]_f)/([B]_o - [B]_f)$ will yield a straight with a slope of j_2K_b and a non-negative intercept on the ordinate at j_b .

Saturating [B]. An alternative experimental simplification is to set the concentration of substrate B much higher than K_b . In these circumstances, the expressions for v and $[EAB]/[E]'_o$ are identical to Equation (1) and (6) except that Δ is replaced by Δ_b (Equation 13).

$$\Delta_b = 1 + K_a(1 + [Q]/K_{iq})/[A] \quad (13)$$

The quantity $[EA]/[E]'_o$ becomes zero while the remaining distribution equations are given by Equations (14) and (15).

$$[E]/[E]'_o = (K_a/[A])/\Delta_b \quad (14)$$

$$[EQ]/[E]'_o = (K_a[Q]/(K_{iq}[A] + \lambda))/\Delta_b \quad (15)$$

Integrating, setting $[E]'_o = 0$ and rearrangement then gives Equation (16).

$$\frac{V_m}{[A]_o - [A]_f} = K_a(j_1 + j_4[A]_o/K_{iq}) \frac{\ln([A]_o/[A]_f)}{[A]_o - [A]_f} + j_b - j_4K_a/K_{iq} \quad (16)$$

Plotting $V_m/([A]_o - [A]_f)$ against $\ln([A]_o/[A]_f)/([A]_o - [A]_f)$ gives a family of straight lines with a slope that increases in a linear fashion with the initial concentration of substrate A. These lines meet on the ordinate at a value of $j_b - j_4K_a/K_{iq}$ that is not constrained to be positive.

Materials and methods

L. mesenteroides G6P dehydrogenase, G6P, NAD^+ , $NADP^+$ and $NADPH$ were purchased from the Sigma Chemical Company (St. Louis, MO, USA). Other chemicals were obtained from local commercial suppliers. For steady-state kinetic measurements, reactions contained G6P, NAD^+ (or $NADP^+$) and $NADPH$ concentrations as required for the particular experiment, and 0.025% (*w/v*) sodium dodecyl sulphate (SDS) in 0.1 M Tris-HCl buffer (pH 7.8). Reactions were initiated by adding the enzyme and followed at 340 nm and 30°C. For inactivation experiments, the enzyme was incubated at 30°C in the desired buffer and the residual activity was measured by taking samples at timed intervals. These were then added to reaction mixtures as above, but omitting SDS to prevent further inactivation, and the initial velocity was measured. End-point assays used a similar procedure to steady-state kinetic measurements except that the reaction was followed to completion at a wavelength (≥ 340 nm) chosen so that the total change in absorbance was no greater than 1.5. Using the spectrum of authentic $NAD(P)H$ as a reference, the amount formed in the reaction was determined.

Results

G6P dehydrogenase from *L. mesenteroides* is a fairly stable enzyme. In order to induce instability for the purpose of testing the theory outlined above, SDS (0.025%, *w/v*), was added. Under these conditions the enzyme is unstable, showing a first-order loss of activity for at least three half-lives (Figure 1). The rate constant for activity loss is $3.83 \pm 0.06 \text{ h}^{-1}$. Addition

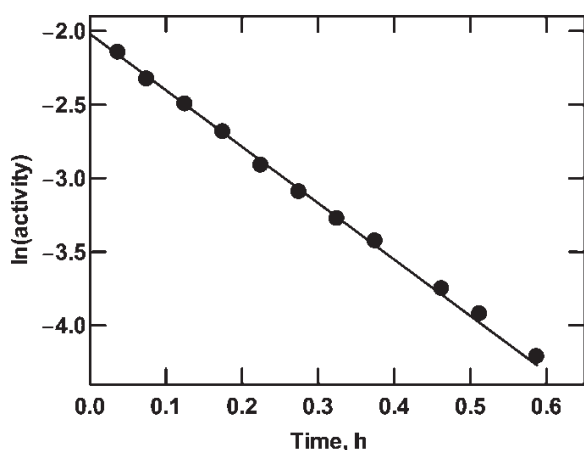


Figure 1. Inactivation of G6P dehydrogenase. Enzyme was incubated at 30°C in 0.1 M Tris-HCl (pH 7.8) containing 0.025% (*v/v*) SDS. At intervals, samples were removed and assayed for residual activity. The initial activity was 0.22 U/mL.

of a saturating (10 mM) concentration of NAD^+ destabilizes the enzyme somewhat (data not shown), increasing the inactivation rate constant to $9.74 \pm 0.37 \text{ h}^{-1}$. In contrast, both NADH and NADPH results in some stabilization (data not shown); for the latter compound, the inactivation rate constant decreases to $1.43 \pm 0.09 \text{ h}^{-1}$.

One result of this instability is that after prolonged incubation of the enzyme with limiting [G6P] (substrate B) and excess [NAD^+] (substrate A), the amount of NADH formed is less than the amount of G6P initially present (Figure 2). The extent of reaction appears to be proportional to the initial concentration of G6P with the slope inversely related

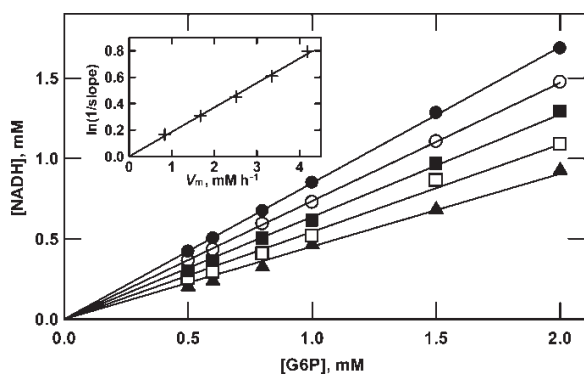


Figure 2. Product formation by G6P dehydrogenase at saturating NAD^+ . Reactions were as described in the text, containing 10 mM NAD^+ , G6P as shown (0.5 to 2.0 mM) and initial enzyme concentrations of 70 (●), 56 (○), 42 (■), 28 (□) and 14 (▲) mU/mL. A straight line passing through the origin was fitted by linear regression to the data at each enzyme concentration to determine the slope. As shown in the inset, the value of $\ln(1/\text{slope})$ is proportional to the enzyme concentration.

to the amount of enzyme added. When $\ln(1/\text{slope})$ is plotted against the quantity of enzyme, the results are described by a straight line passing through the origin (Figure 2, inset).

It has been shown previously [1] that the results seen in Figure 2 are characteristic of an unstable enzyme that forms a stable enzyme-substrate complex. In terms of Equation (11), j_b would be zero while j_2 would be finite. This interpretation received further support when the results shown in Figure 2 were used to construct a plot (Figure 3) of $V_m/([G6P]_o - [G6P]_t)$ versus $\ln([G6P]_o/[G6P]_t)/([G6P]_o - [G6P]_t)$. It is clear that irrespective of the initial G6P and enzyme concentration, a common straight line describes all of the data, which is consistent with Equation (11). Moreover, the intercept on the ordinate (j_b) is close to zero, confirming the conclusion drawn from Figure 2. Assuming that the line in Figure 3 passes through the origin, its slope ($j_2 K_b$) was estimated. Knowing that K_b is equal to 0.550 mM (determined from steady-state kinetic measurements, data not shown) yields a value for j_2 of $9.507 \pm 0.130 \text{ h}^{-1}$. Two further repetitions of this experiment gave similar results: $8.307 \pm 0.183 \text{ h}^{-1}$ and $9.017 \pm 0.206 \text{ h}^{-1}$; analysis of the combined results from three experiments gave a value for j_2 of $8.953 \pm 0.114 \text{ h}^{-1}$.

As mentioned earlier, j_b is a composite rate constant (Equation 12) that depends on the values of j_3 , j_4 and λ . In order to separate j_4 from j_b , a second series of experiments was performed in which the concentration of the pyridine nucleotide was varied while maintaining G6P at a high and saturating concentration. To avoid very high substrate concentrations, these experiments were performed using NADP^+ rather than NAD^+ because the former has a much lower Michaelis constant. The results from one such experiment are shown in Figure 4 from which it is clear that the data fall on a series of straight lines with

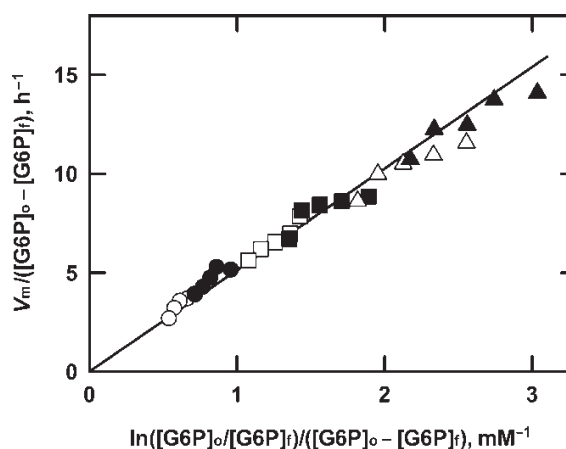


Figure 3. Analysis of product formation by G6P dehydrogenase at saturating NAD^+ . The data from Figure 2 are plotted according to Equation (11).

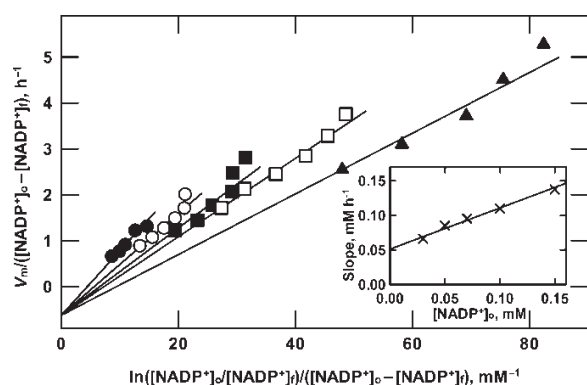


Figure 4. Analysis of product formation by G6P dehydrogenase at saturating G6P. Reactions were as described in the text, containing 10 mM G6P and 150 (●), 100 (○), 70 (■), 50 (□) or 30 (▲) μM NADP^+ . For each concentration of NADP^+ the enzyme concentration was varied from 0.69 to 2.76 mU/mL , to obtain the series of data points shown along each line shown. Data are plotted according to Equation (16). As shown in the **inset**, the slope of the lines in the main graph is proportional to the NADP^+ concentration.

a common intercept on the ordinate below the origin and with slopes that depend on the initial concentration of NADP^+ . This is in accord with Equation (16), which requires that the slopes of the lines should be a linear function of the initial concentration of NADP^+ ; as shown in the inset to Figure 4, this prediction is borne out by the data.

Equation (16) may be considered to be defined by three independent parameters; $j_1 K_a$, $j_4 K_a / K_{iQ}$ and j_b . I have determined K_a (11.9 μM) and K_{iQ} (20.1 μM) from steady-state kinetic measurements so the data shown in Figure 4 may be used to estimate j_1 , j_4 and the composite rate constant, j_b . The results of such an analysis are shown in the first row of Table I as experiment '1'.

The value of j_b is not well determined with a standard error more than five times the value. Moreover, j_b is negative which is physically meaningless. This is because the definition of λ is such that it must lie in the range 0 to 1; therefore j_b can only fall

Table I. Analysis of G6P dehydrogenase inactivation during catalysis with saturating G6P. Reactions were as described for Figure 4. Data from experiment 1 were analyzed by nonlinear regression using Equation (16) to obtain best fit values and standard errors for j_1 , j_4 and j_b (row 1) The latter was found to be close to zero so the data were reanalyzed with $j_b = 0$ (row 2). Experiments 2 (row 3) and 3 (row 4), and the combined results from all three experiments (row 5) were also analyzed with $j_b = 0$.

Experiment	j_1 (h^{-1})	j_4 (h^{-1})	j_b (h^{-1})
1	4.245 ± 0.171	1.037 ± 0.144	-0.008 ± 0.043
	4.236 ± 0.160	1.020 ± 0.110	0
2	3.390 ± 0.486	1.720 ± 0.343	0
3	4.006 ± 0.319	1.396 ± 0.220	0
1 + 2 + 3	4.021 ± 0.168	1.283 ± 0.116	0

in the range j_3 to j_4 (Equation 12) and must therefore be positive. The most reasonable interpretation, and one that agrees with the conclusions drawn from Figures 2 and 3, is that $j_b = 0$.

The data were reanalyzed with this constraint to obtain the results shown in the second row of Table I. Two further experiments (Table I, experiments 2 and 3) gave similar results to experiment 1 and the three sets of data were combined to give overall estimates of j_1 and j_4 (Table I, bottom row).

Discussion

Values for the four inactivation rate constants (j_1 , j_2 , j_b and j_4) of Equations (11) and (16) have been determined. Although j_3 has not been measured, the fact that j_b is zero implies that $j_3 = 0$, since j_b must lie between j_3 and j_4 (Equation 12) and the latter is finite. It follows that λ must be close to zero, which will occur when catalysis (k_5) is much slower than the rate constant for release of the lactone product (k_7). The best estimates of the four inactivation rate constants are: $j_1 = 4.02 \pm 0.17 \text{ h}^{-1}$, $j_2 = 8.95 \pm 0.11 \text{ h}^{-1}$, $j_3 = 0 \text{ h}^{-1}$, and $j_4 = 1.28 \pm 0.12 \text{ h}^{-1}$.

The rate constants j_1 , j_2 and j_4 correspond to the inactivation of free enzyme (E), EA and EQ (Scheme 1). These rate constants could be confirmed independently by directly measuring inactivation of the enzyme when it was incubated under the appropriate conditions. One such experiment was shown in Figure 1. The rate constant for loss of activity in the absence of substrates ($3.83 \pm 0.06 \text{ h}^{-1}$) should correspond to j_1 ($4.02 \pm 0.17 \text{ h}^{-1}$, Table I) and there is good agreement between the values. In the presence of a saturating concentration of substrate A, the rate constant for inactivation was estimated to be $9.74 \pm 0.37 \text{ h}^{-1}$, in reasonable agreement with the value of j_2 determined from Figure 3 ($8.95 \pm 0.11 \text{ h}^{-1}$). Similarly, the value for j_4 ($1.28 \pm 0.12 \text{ h}^{-1}$) should correspond to the inactivation rate constant for the enzyme saturated with Q. This rate constant was determined to be $1.43 \pm 0.09 \text{ h}^{-1}$.

The values of j_1 , j_2 and j_4 are of a comparable magnitude, all in the range 1 to 10 h^{-1} . In contrast, $j_3 = 0$ is very much lower and seems to be close to zero. Why should the EAB complex be stable while each of the other enzyme forms in the catalytic cycle is susceptible to inactivation? In E, EA and EQ the active site must be open in order to admit entrance of a substrate or release of a product. However, in the ternary EAB complex, catalysis occurs. Thus it appears that the closure of the active site gives added stability to the enzyme.

Here I have shown that it is possible to extend the theory and analysis of unstable enzymes [1] to those with two substrates. The theory was employed to analyze an enzyme catalyzing an ordered sequential mechanism. However, there is no reason why it could

not be applied to enzymes with random or ping-pong mechanisms, or those where both products are kinetically significant. The equations would differ somewhat but the basic principles outlined here would remain the same. The process would involve the following steps.

- (1) Write down expressions for the fraction of enzyme present as each of the molecular species in the catalytic cycle. Computer programs are available to automate this process (e.g. [14]).
- (2) Use these distribution equations to write down the overall rate equation ($d[A]/dt$) for the reaction mechanism.
- (3) Use these distribution equations to write down the overall rate of enzyme inactivation, $d[E]_0'/dt$.
- (4) Combine these two differential equations to determine $d[E]_0'/dtA$.
- (5) Integrate and simplify for experimental conditions that can be achieved in practice.

Acknowledgements

Some of the experiments reported here were performed by Stephen Pike.

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